

Using trig and the fact that the two triangles have a common side, we can write:

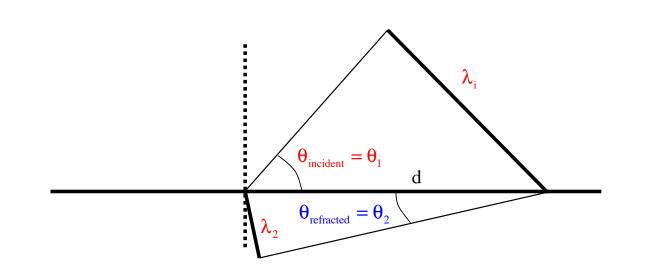
$$d = \frac{\lambda_1}{\sin \theta_1} = \frac{\lambda_2}{\sin \theta_2}$$

Noting that the relationship between frequency, wavelength and wave speed is:

$$v = \lambda v \implies \lambda = \frac{v}{v}$$

Additionally:

5.)



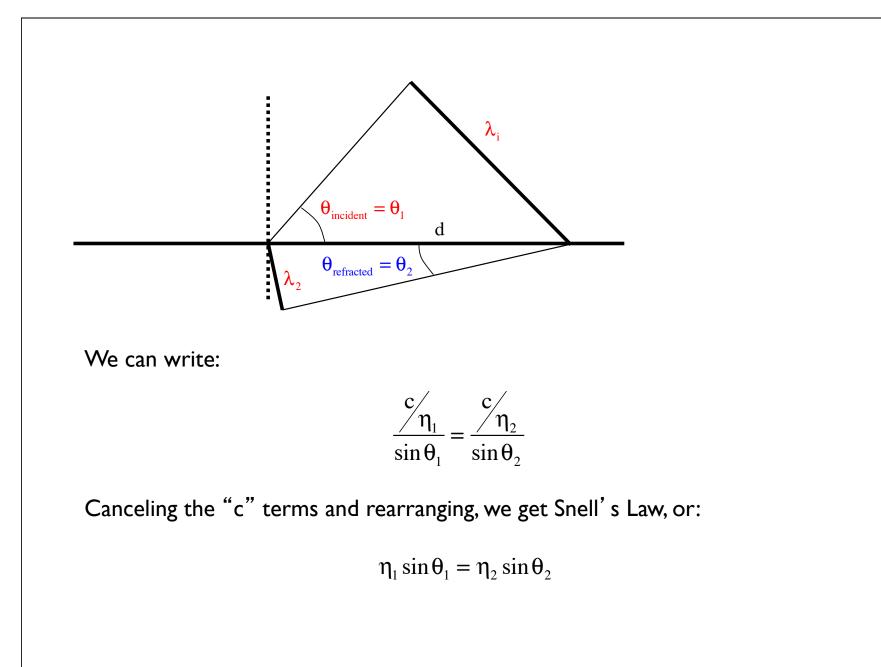
Noting that the frequency is the same no matter where the wave is, and remembering that the velocity is different in each medium, we can rewrite this "d" relationship as:

$$d = \frac{\frac{v_1}{v}}{\sin \theta_1} = \frac{\frac{v_2}{v}}{\sin \theta_2}$$

Canceling the frequency terms, then defining the index of refraction η as the ratio of the speed of light "c" to the effective speed of the wave in the material "v", or:

$$\eta_1 = \frac{c}{v_1} \implies v_1 = \frac{c}{\eta_1}$$

6.)



7.)